

Analog VLSI Biophysical Neurons and Synapses With Programmable Membrane Channel Kinetics

Theodore Yu, *Student Member, IEEE*, and Gert Cauwenberghs, *Senior Member, IEEE*

Abstract—We present and characterize an analog VLSI network of 4 spiking neurons and 12 conductance-based synapses, implementing a silicon model of biophysical membrane dynamics and detailed channel kinetics in 384 digitally programmable parameters. Each neuron in the analog VLSI chip (NeuroDyn) implements generalized Hodgkin-Huxley neural dynamics in 3 channel variables, each with 16 parameters defining channel conductance, reversal potential, and voltage-dependence profile of the channel kinetics. Likewise, 12 synaptic channel variables implement a rate-based first-order kinetic model of neurotransmitter and receptor dynamics, accounting for NMDA and non-NMDA type chemical synapses. The biophysical origin of all 384 parameters in 24 channel variables supports direct interpretation of the results of adapting/tuning the parameters in terms of neurobiology. We present experimental results from the chip characterizing single neuron dynamics, single synapse dynamics, and multi-neuron network dynamics showing phase-locking behavior as a function of synaptic coupling strength. Uniform temporal scaling of the dynamics of membrane and gating variables is demonstrated by tuning a single current parameter, yielding variable speed output exceeding real time. The 0.5 μm CMOS chip measures 3 mm \times 3 mm, and consumes 1.29 mW.

Index Terms—Neuromorphic engineering, reconfigurable neural and synaptic dynamics, silicon neurons, subthreshold metal–oxide semiconductor (MOS), translinear circuits.

I. INTRODUCTION

NEUROMORPHIC engineering [1] takes inspiration from neurobiology in the design of artificial neural systems in silicon integrated circuits (ICs), based on the function and structural organization of biological nervous systems. By emulating the form and architecture of biological systems, neuromorphic engineering seeks to emulate their function as well. Since the first silicon model of a biophysical neuron in 1990 [2], great advances have been made in the detail and scale of the modeling the neural function in silicon. Recently, the focus of the neuromorphic engineering effort in silicon modeling of the nervous system has shifted from the sensory periphery to central nervous

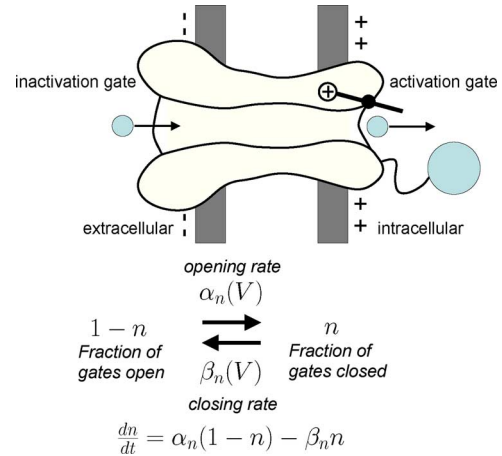


Fig. 1. An ion membrane channel is pictured [13] (top) with an accompanying mathematical expression (bottom) describing the channel kinetics in terms of the opening α and closing β rates.

function addressing higher levels of integration and cognitive processing in the cortex and other brain regions [3]–[6], setting the stage for further advances toward closed-loop integration of biological and silicon neural systems [8]–[12].

Biophysical modeling and implementation of the neural function require a careful account of channel opening and closing kinetics and their role in ion transport through membranes that give rise to the rich neuronal and synaptic dynamics observed in neurobiology [13] (Fig. 1). Hodgkin and Huxley's seminal work in the investigation and formalization of neuron membrane dynamics have long been the standard of biophysical accuracy [14]. The difficulty of realizing the complex functional form of the Hodgkin–Huxley membrane currents and channel variables in analog circuits has motivated alternative realizations by simplifications in the model [15]–[18]. The prevailing approach in neuromorphic engineering design has been to abstract the neuron membrane action potential to discrete-time spike events in simplified models that capture the essence of integrate-and-fire dynamics and synaptic coupling between large numbers of neurons in an address-event representation [19]–[25]. The advantage of these approaches is that they support event-based interchip communication, including direct input from neuromorphic audition [26] and vision [27] sensors, and may lead to highly efficient and densely integrated implementations in analog very-large scale integrated (VLSI) silicon [28], [29].

Here, we offer an alternative neuromorphic engineering approach that targets applications where biophysical detail in modeling neural and synaptic dynamics at the level of channel kinetics is critical. Examples of these applications include modeling of the effect of neuromodulators, neurotoxins, as well as neurodegenerative diseases on neural and synaptic

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T. Yu is with the Department of Electrical and Computer Engineering, Jacobs School of Engineering, University of California, San Diego, CA 92039 USA. He is also with the Institute for Neural Computation, University of California, San Diego, CA 92039 USA (e-mail: teyu@ucsd.edu).

G. Cauwenberghs is with the Department of Bioengineering, Jacobs School of Engineering, University of California, San Diego, CA 92039 USA. He is also with the Institute for Neural Computation, University of California, San Diego, CA 92039 USA (e-mail: gert@ucsd.edu).

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function through parameter changes in the channel kinetics. For these and other applications in computational neuroscience, a direct correspondence between the parameters governing the biophysics of neural and synaptic function and those in the implemented computational model is greatly beneficial [30]–[33]. The approach we propose here is the first in analog VLSI to fully model the general voltage dependence of rate kinetics in the opening and closing of membrane ion channels. We illustrate this approach with the implementation and demonstration of *NeuroDyn*, an analog VLSI network of four neurons and 12 chemical synapses with a total of 384 digitally programmable parameters governing the channel conductance, reversal potential, and opening and closing kinetics voltage profile of 24 individually configurable channel variables.

Hodgkin and Huxley in their landmark paper [14] resorted to heuristics in curve-fitting the rate kinetics of channel variables observed through ingenious measurements on the squid giant axon. Any model replicating the precise functional form of this heuristic fit would, at best, produce an approximation to squid giant axons. To a large extent, the variety in dynamics between different neuron types in different organisms as well as the anomalies due to biomolecular agents and neurodegenerative processes acting on membrane channels arise from the resulting differences in channel properties. These channel properties are compactly characterized in our model by 16 ($7 + 7 + 1 + 1$) parameters for each channel variable specifying the voltage dependence of channel opening and closing rates (seven regression points each), besides values for the channel conductance and reversal potential. Fewer parameters would impair the flexibility in modeling neural and synaptic diversity in healthy and diseased nervous systems, although fewer parameters would be appropriate in special purpose implementations of specific model instances and their functional abstractions [34]–[38] where the application warrants efficiency rather than flexibility and biophysical explanatory power in parameter selections. Likewise, extensions to the models to incorporate further biophysical detail, such as short-term synaptic adaptation [39]–[42] and multicompartmental dynamics through linear [43] and nonlinear [44] dendritic coupling would incur larger numbers of parameters where the need for the extended models justifies the increase in implementation complexity.

While the implementation of parameterized channel kinetic rate equations in *NeuroDyn* provides the capacity to model a large variety of neuron and synapse behaviors, it requires tuning over a large number of parameters. Since each of these parameters has a direct physical correspondence in channel kinetics and membrane dynamics, values for these parameters can be obtained from physical considerations and measurements. Fine tuning of these parameters, to account for uncertainties in the modeling as well as imprecisions in the implemented model, would still be desirable. Extensive parameter fine-tuning was found to be unnecessary to address transistor mismatch. A simple calibration and parameter fitting procedure proved adequate to counteract mismatch and nonlinearities in setting parameters in the biophysical model to desired values. The correspondence between biophysical and circuit parameters is described in Section IV, with experimental alignment documented

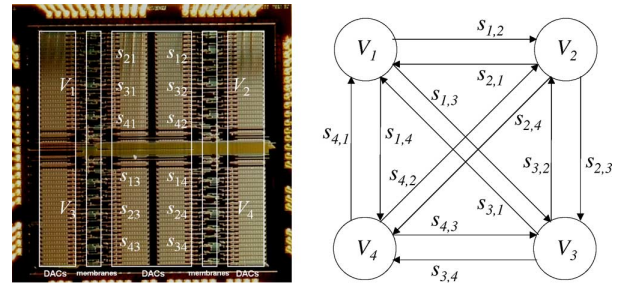


Fig. 2. *NeuroDyn* chip micrograph. (a, top left) and system diagram (b, top right). Four neurons are interconnected with 12 synapses, each with programmable channel kinetics, conductances, and reversal potentials (see Table I).

in Section V and the parameter alignment procedure detailed in Appendix B.

In the present implementation, we have aimed for functional flexibility and real-time control over parameters and internal dynamics, rather than efficiency and density of integration. The *NeuroDyn* system interfaces through the universal serial bus (USB) to Matlab software on a workstation to update the 384 parameters in real time, and to continuously control and observe each of the four membrane potentials and 24 channel variables. To support this level of programmability, all parameters are stored locally on-chip in digital registers interfacing to a bank of 384 current multiplying digital-to-analog converters (DACs). The neuromorphic modeling approach presented here is extendable to other implementations where parameters may be shared across individual neurons and/or channels for greater efficiency, and combined with floating-gate nonvolatile analog storage [45]–[51] or dynamically refreshed volatile analog storage [52] of the parameters for greater density of integration. For example, central pattern generators require only a few neurons for implementation, yet they can characterize complex behavior [11].

We envisage *NeuroDyn* as an enabling tool for computational and systems neuroscience, since all internal dynamical variables and their parameters are grounded in the biophysics of membranes and ion channels. With its analog interface to the physical world, the *NeuroDyn* chip (Fig. 2) may also serve as an electronic training tool for budding neuroscientists and neurobiologists to practice patch clamp recording and other experimental techniques on “virtual” neurons. The *NeuroDyn* system contains various analog and digital exposed probes in the circuit board that allow for a real-time interface to the internal membrane potential and channel dynamics.

Furthermore, the low-power and efficient circuit implementation, combined with extensions for hardcoded parameter settings or high-density analog storage, support applications of the device as an implantable computational neural interface *in vivo*. These approaches, as described in [7], have great potential in the realization of intelligent neural prostheses when combined with embedded signal processing to process incoming neural spike data streams [8], [9] and activate prostheses [10], [12].

The analog VLSI design of the *NeuroDyn* system, and preliminary experimental results were presented in [53]. First results on coupled neural dynamics with inhibitory synapses were reported in [54]. Here, we provide details on the circuit implemen-

TABLE I
NEURODYN DAC PARAMETERS

Neurons V_i :			
$\alpha_{n_i}(V)$	$\beta_{n_i}(V)$	g_{Na_i}	E_{Na_i}
$\alpha_{m_i}(V)$	$\beta_{m_i}(V)$	g_{K_i}	E_{K_i}
$\alpha_{h_i}(V)$	$\beta_{h_i}(V)$	g_{L_i}	E_{L_i}
4x3x7*	4x3x7*	4x3	4x3
Synapses s_{ij} :			
$\alpha_{r_{ij}}(V_{pre})$	$\beta_{r_{ij}}(V_{post})$	$g_{syn_{ij}}$	$E_{syn_{ij}}$
12x7*	12x7*	12	12

* All rates α, β are functions of voltage as 7-point sigmoidal splines (Section IV-A-1).

tation and complete experimental characterization of the neural and synaptic circuits, and present calibration and parameter-fitting procedures to align neural and synaptic characteristics from models or recorded data onto the digitally programmable analog hardware. We demonstrate the operation of the system by replicating opening and closing rates, gating variable kinetics, and action potentials of the Hodgkin–Huxley model, and study the dynamics of a network of two neurons coupled through reciprocal inhibitory synapses.

II. NEURODYN ARCHITECTURE

A. System Overview

The *NeuroDyn* board consists of four Hodgkin–Huxley (HH)-based neurons fully connected through 12 conductance-based synapses as shown in Fig. 2(b). All parameters are individually addressable and individually programmable and are biophysically based governing the conductances, reversal potentials, and voltage dependence of the channel kinetics. There are a total of 384 programmable parameters governing the dynamics as shown in Table I. Each parameter is stored on-chip in a 10-b DAC.

B. Chip Architecture

The *NeuroDyn* chip is organized into four quadrants with each quadrant containing one neuron, and three synaptic inputs from the other neurons. Each neural and synaptic membrane channel current follows the same general form as illustrated in Fig. 3. Each channel current is a product of a conductance term modulated by a product of gating variables and the difference between the membrane voltage and reverse potential as in (2). The similar form for the neuron channel currents and synaptic current allows for a small number of circuits to model each component of the channel current.

III. BIOPHYSICAL MODELS

A. Membrane Dynamics

The HH membrane dynamics [14], including conductance-based synaptic input, are described by

$$C_{mem} \frac{dV_i}{dt} = -I_{Na_i} - I_{K_i} - I_{L_i} - \sum_j I_{syn_{ij}} \quad (1)$$

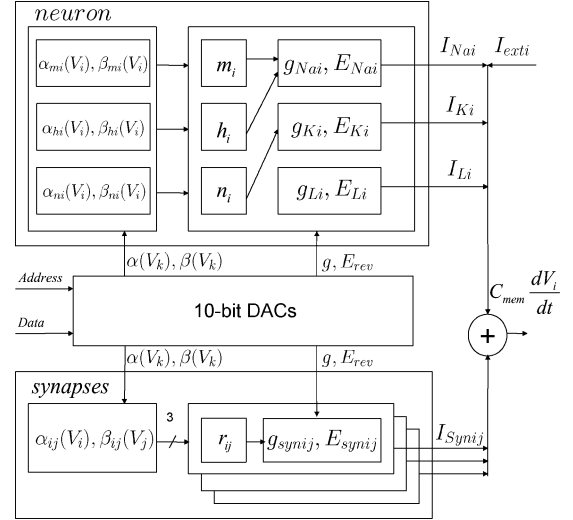


Fig. 3. System diagram for one of the four neurons in the *NeuroDyn* chip.

where $i, j = 0 \dots 3$, and

$$\begin{aligned} I_{Na_i} &= m_i^3 h_i g_{Na_i} (V_i - E_{Na_i}) \\ I_{K_i} &= n_i^4 g_{K_i} (V_i - E_{K_i}) \\ I_{L_i} &= g_{L_i} (V_i - E_{L_i}) \\ I_{syn_{ij}} &= r_{ij} g_{syn_{ij}} (V_i - E_{syn_{ij}}). \end{aligned} \quad (2)$$

All of the conductances in the model, including the synaptic conductances $g_{syn_{ij}}$, are positive. Excitatory synapses are characterized by reversal potentials $E_{syn_{ij}}$ above the rest potential, whereas for inhibitory synapses, the reversal potential $E_{syn_{ij}}$ is below the rest potential.

B. Channel Kinetics

The neuron channel gating variables n_i, m_i , and h_i , as in the HH neuron formulation, are modeled by a rate-based first-order approximation to the kinetics governing the random opening and closing of membrane channels

$$\frac{dn_i}{dt} = \alpha_{n_i}(1 - n_i) - \beta_{n_i}n_i \quad (3)$$

$$\frac{dm_i}{dt} = \alpha_{m_i}(1 - m_i) - \beta_{m_i}m_i \quad (4)$$

$$\frac{dh_i}{dt} = \alpha_{h_i}(1 - h_i) - \beta_{h_i}h_i \quad (5)$$

where the three channel variables n_i, m_i , and h_i for each neuron i denote the fractions of corresponding channel gates in the open state, and where the α and β parameters are the corresponding voltage-dependent opening and closing rates.

Similarly, the synaptic channel currents are modeled by using first-order kinetics in the receptor variables r_{ij} , the fraction of receptors in the open state [55]

$$\frac{dr_{ij}}{dt} = \alpha_{r_{ij}}(1 - r_{ij}) - \beta_{r_{ij}}r_{ij}. \quad (6)$$

The opening rates $\alpha_{r_{ij}}$ are dependent on presynaptic voltage V_j , modeling the release of the neurotransmitter and its binding at the postsynaptic receptor, affecting the channel opening. In

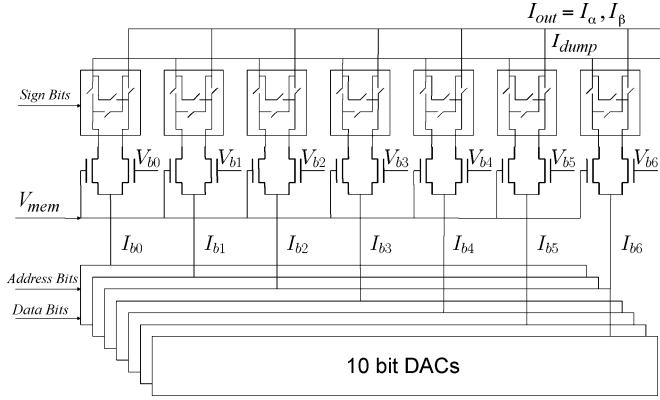


Fig. 4. Generalized channel rate variables α and β implemented in the current domain with additive seven-point sigmoidal functions. Programmable parameters scaling the sigmoidal currents are stored in 10-b MOSFET-only R-2R DACs with additional bit governing polarity.

contrast, the closing rates $\beta_{r_{ij}}$ are generally dependent on post-synaptic voltage V_i . For non-NMDA synapses, this dependence is a constant, given the rate of unbinding and resulting decrease in the channel conductance following presynaptic deactivation. For NMDA synapses, this dependence models the effect of magnesium blocking of synaptic conductance triggered by postsynaptic potential.

The point of departure from the prevailing models in computational neuroscience is that the channel gate/receptor opening and closing rates are not specified and implemented as analytic functions, but are parameterized as regression functions, leaving significant flexibility in accommodating diversity in channel properties in the implemented model.

IV. NEUROMORPHIC IMPLEMENTATION AND CHARACTERIZATION

A. Voltage-Dependent Channel Kinetics

1) *Seven-Point Sigmoidal Spline Regression:* Opening rates α and closing rates β are modeled and regressed as 7-point additive spline sigmoidal functions implemented in the circuit illustrated in Fig. 4. Each sigmoid in the regression spline is implemented by a simple differential pair of metal-oxide semiconductor (MOS) transistors operating in subthreshold, where a bias current scales the sigmoid while a bias voltage determines the sigmoid offset [1]. These bias voltages are linearly spaced and are set through a voltage divider resistor string. A programmable 10-b metal-oxide semiconductor field-effect transistor (MOSFET)-only R-2R digital-to-analog converter (DAC) supplies the bias currents. An additional sign bit controls a switch circuit that determines the polarity of the output current slope, which selects either monotonically increasing or monotonically decreasing voltage dependence. The output currents from each differential pair are then additively combined to provide the composite function for the opening or closing rate. Each of the spline amplitudes and sign selection bits are individually programmable. By properly setting the current bias values and sign bit for each of the seven sigmoidal

functions, the summation can accommodate a wide range of functions approximating typical rate functions α and β

$$I_{out}(V) = \sum_{k=1}^7 I_{bk} I_{\sigma,k}(V) = \sum_{k=1}^7 \frac{I_{bk}}{1 + e^{\pm \kappa (V_{bk} - V)/V_T}} \quad (7)$$

where the output current I_{out} denotes either one of the I_α and I_β rates, and where $V_T = kT/q$ is the thermal voltage.

To enforce a consistent temporal scale of the dynamics across membrane and gating variables, the currents implementing the opening and closing rates as well as the membrane conductances are globally scaled with a current I_τ that drives the multiplying DACs

$$I_\alpha = \alpha I_\tau \quad (8)$$

$$I_\beta = \beta I_\tau \quad (9)$$

$$I_g = g I_\tau \quad (10)$$

and, thus, uniformly controls the time base of all dynamic variables with a global temporal scale parameter $\tau = CV_T/I_\tau$.

2) *Programmable Channel Kinetics:* The gate opening and closing variables for one neuron were programmed to implement the HH model (Section III), with the target functions for the channel kinetics defined according to the HH opening and closing rate functions. The sigmoidal spline functions were measured from the chip to provide the basis functions at each spline location. Rectified linear least-squares optimization was then applied to determine the current bias parameters based on chip characteristics. Further parameter fitting details are provided in Appendix B. The 10-b programming for each of the seven spline amplitude levels in the regression functions results in the fit illustrated in Fig. 5. The closeness of fit is limited by the dynamic range of the 10-b DACs to simultaneously fit the steep slope of the m_β gating variable and the gradual slopes of the h_α and n_β parameters. Parameter fitting was achieved by applying rectified linear regression and iterative linear least-squares residue correction as described in Appendix B.

B. Gated Conductances

Gating variables m_i , h_i , n_i , and r_{ij} are implemented as currents by the log-domain circuit shown in Fig. 6, which implements the kinetics (3)–(6) as

$$CV_T \frac{d}{dt} \frac{I_{out}}{I_{ref}} = I_\alpha \left(1 - \frac{I_{out}}{I_{ref}} \right) - I_\beta \frac{I_{out}}{I_{ref}} \quad (11)$$

where I_{out} represents the gating variable output current, and where I_{ref} is a current reference that only affects the amplitude scale of the gating variables, but not the temporal scale of their dynamics.

The use of MOS transistors operating in the subthreshold region allows analog multiplication through the exponential relationship between the transistor input voltage and output current in translinear circuits [56]. The addition of the capacitor transforms the circuit from a translinear multiplier into a log-domain filter [59] that implements the desired first-order dynamics. The derivation is provided in Appendix A.

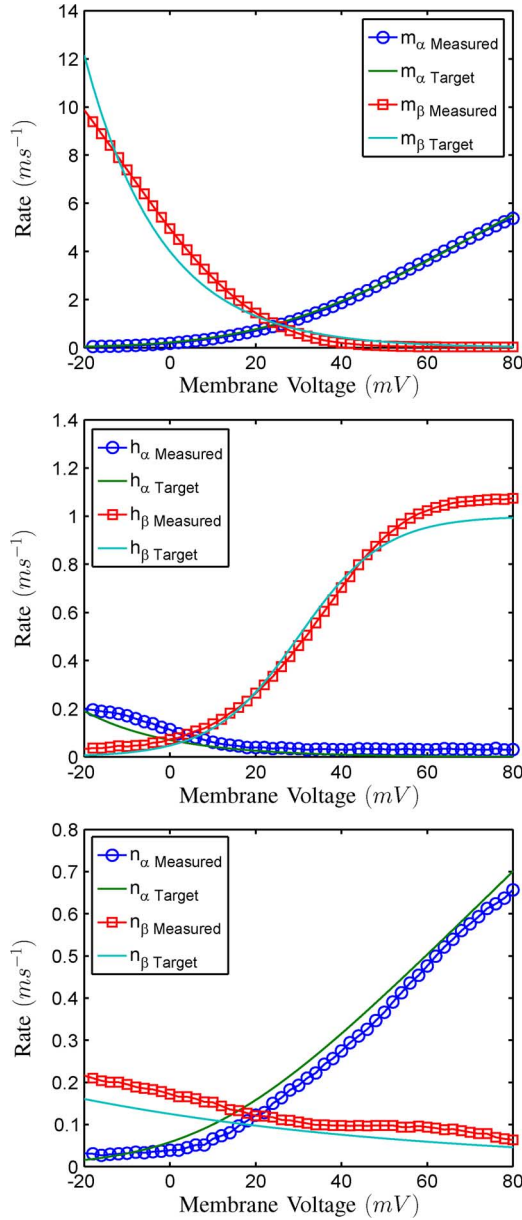


Fig. 5. Target and measured channel opening and closing rates α and β for gating variables n , m , and h of a single *NeuroDyn* neuron approximating the HH model, obtained by fitting the on-chip programmed parameters to the HH model.

The circuit is similar in implementation complexity to a previous implementation of rate kinetics [33] but avoids the backgate effect in the bulk CMOS process on the linearity in the first-order dynamics, and provides full programmability in the voltage profile of the dynamics. The circuit offers 14 parameters, specifying the detailed voltage dependence of the opening and closing rates offering flexibility in accurately modeling the channel kinetics.

1) *Steady-State (in)Activation Functions*: The steady-state (in)activation functions for one *NeuroDyn* programmed to replicate the HH model are shown in Fig. 7. These data were gathered by clamping the membrane voltage and slowly sweeping the membrane voltage while recording the values for the m , h , and n gating variables. The results closely match the expected steady-state values according to the HH model [14]. Notice that

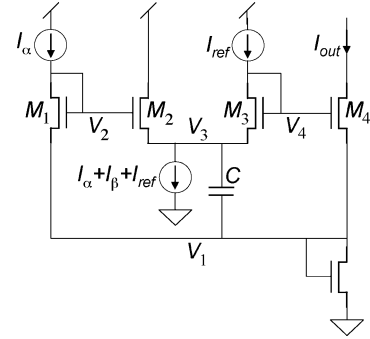


Fig. 6. Log-domain circuit implementing channel kinetics (3)–(6).

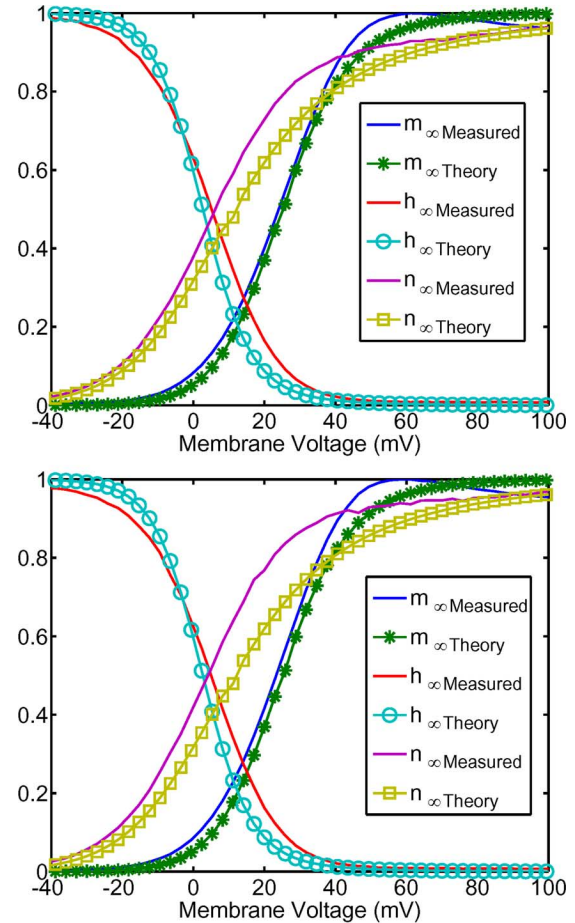


Fig. 7. Steady-state (in)activation functions measured on one neuron of *NeuroDyn* programmed to replicate the HH model (a) for fast setting of the neuron parameters and (b) for slow setting of the parameters, obtained without recalibration by increasing the global temporal scale parameter I_τ 2.5-fold.

there is little variation between the fast and slow time-scale implementations obtained by varying the global temporal scale parameter I_τ . This desirable time independence in the steady state (in)activation functions is clearly reflected in Fig. 7.

2) *Voltage-Dependent Time Constants*: The measured voltage-dependent time constants of the implemented HH model are shown in Fig. 8. The time constants were estimated by averaging the measured rise and fall times of changes in the gating variables under alternating small-amplitude voltage steps around the swept membrane voltage. The observed dynamics are consistent with the HH model [14] except for the

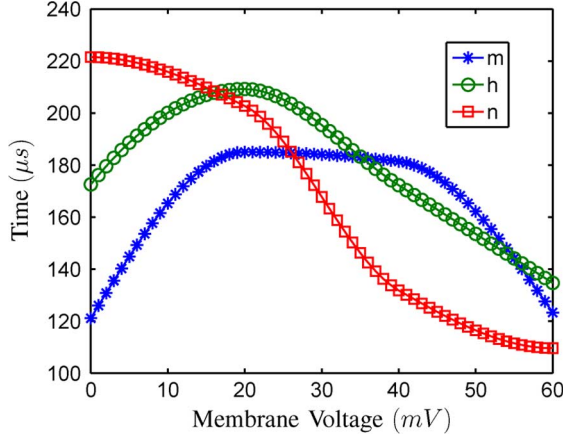


Fig. 8. Voltage-dependent time constants measured for one *NeuroDyn* neuron approximating the HH model.

larger observed time constants of the m gating variable due to delays imposed by the on-chip output buffers.

C. Translinear Multiplier

A translinear multiplier shown in Fig. 9 implements gating of the membrane conductances with the gating variables. A translinear multiplier exploits the zero sum of voltages along a loop to implement a multiplication of current sources [57] and [56]

$$I_{m^3h g_{Na}} = I_g \left(\frac{I_m}{I_{ref}} \right)^3 \frac{I_h}{I_{ref}} \quad (12)$$

where I_{ref} is the same current reference controlling the amplitude of the gating variables (11) for dimensionless operation. Similar translinear circuits implement the other gated conductances of the form x^a with $a + 1$ stages, where $x = n$ and $a = 4$ for the K⁺ channel; and $x = r$ and $a = 1$ for the conductance-based synapses.

1) *Channel Conductance Dynamics*: The channel conductance dynamics of an implemented HH model are shown in Fig. 10. The membrane voltage was clamped to the specified voltage levels and then released to measure the conductance dynamics for the Na⁺ and K⁺ channels. The results for the Na⁺ channel show an increase in the magnitude and speed (as seen in the width of the curve) of the curve proportional to the magnitude of the depolarizing voltage step. The results for the K⁺ channel also reflect an increase in magnitude and slope proportional to the magnitude of the depolarizing voltage step.

D. Membrane Dynamics

Each membrane conductance is implemented by a differential transconductance amplifier, linearized through shunting in the differential pairs for wide dynamic range in subthreshold MOS operation [58]. Unity gain connection of the amplifier yields a membrane current

$$I_{Na} = \frac{\kappa}{V_{th}} I_{m^3h g_{Na}} (V_m - E_{Na}). \quad (13)$$

For each of the membrane conductances, one amplifier is connected in parallel as shown in Fig. 11. A capacitance $C_{mem} = C$ on the membrane node realizes the membrane dynamics (1).

V. EXPERIMENTAL RESULTS

A. Neuron Spiking Dynamics

We observed the dynamics of the membrane and gating variables for one neuron programmed to implement the HH model. We also demonstrated temporal control through the variation of the global temporal scale parameter set by current I_τ . As shown in Fig. 12, the variation of I_τ scales the time axis of the waveforms by a factor greater than 2. The amplitude scaling in the gating parameters reflects scaling proportional to I_τ consistent with (8)–(10). We implemented the HH model in one neuron and observed the dynamics of the membrane and gating variables as shown in Fig. 12. A small, constant I_{ext} is applied to the neuron in order to provide dc input inducing spiking dynamics.

B. Synapse Dynamics

To observe the synapse dynamics, we took the spiking HH neuron from before and connected that as a presynaptic input to a synapse. The synapse parameters were configured to implement a $GABA_A$ inhibitory synapse. The configuration is illustrated in Fig. 13(a). The conductance curves of the synapse are shown in Fig. 13(b). The synapse conductance curve was observed to rise quickly in time with the spiking neuron and slowly decay in accordance with the expected behavior.

C. Neuron Network Dynamics

We chose to demonstrate synaptic dynamics using a simple network of two neurons coupled with reciprocal inhibitory synapses as illustrated in Fig. 14. The neuron parameters were configured to implement the channel kinetic rate equations of the HH model. The synapse parameters were configured to implement $GABA_A$ inhibitory synapses. The network was first initialized by disconnecting all of the synaptic connections by setting each synaptic conductance to zero. Then, separate external currents I_{ext1} and I_{ext2} were applied to the neurons V_1 and V_2 , respectively, to induce spiking behavior. The values for I_{ext1} and I_{ext2} were chosen so that there was a small difference in the spiking frequency between the two neurons. Then, the synaptic conductances were increased until coupling was observed between the neurons, in the form of phase-locking. The resulting waveforms are shown in Fig. 15. Notice that especially in the oscilloscope capture from the coupled neurons, that there is observable timing jitter in the spiking neuron waveforms. This phase noise is primarily due to the noise intrinsic in the analog circuit implementation. Noise has also been observed in *in vivo* recordings of neuronal activity that can be attributed to thermal, stochastic, and other sources [60]. Thus, the noise from the circuit implementation may prove advantageous to provide a more biorealistic implementation.

VI. CONCLUSION

We presented an analog VLSI network of biophysical neurons and synapses that implements general detailed models of

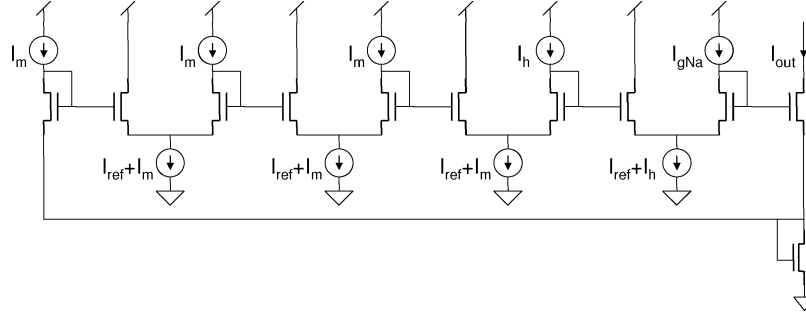


Fig. 9. Translinear circuit implementing gated conductances of the form $x^3 y g$ such as $m^3 h g_{Na}$ and $n^4 g_K$. Synaptic gated conductances $r g_{syn}$ are implemented by a two-stage version of the five-stage translinear circuit shown.

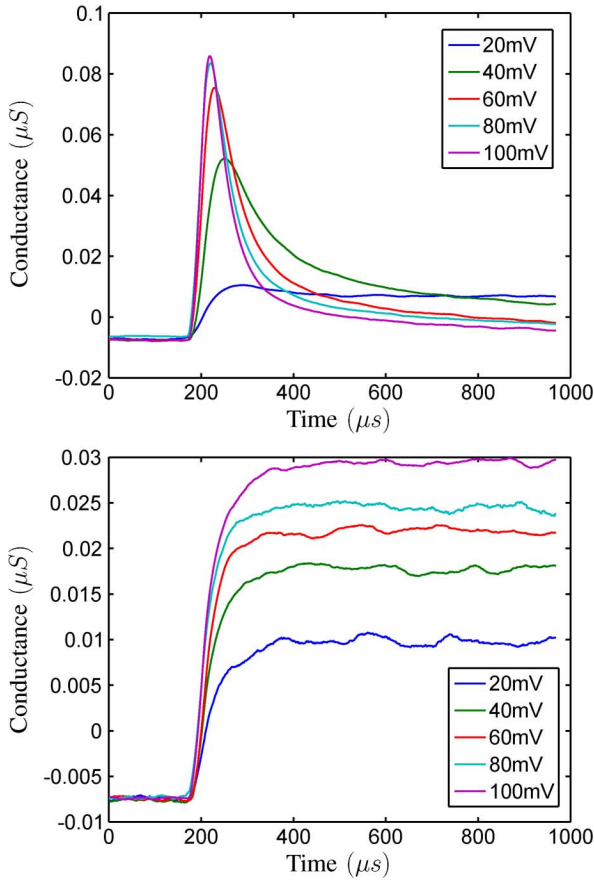


Fig. 10. Channel conductance dynamics measured from one *NeuroDyn* neuron approximating the HH model. (a) for the Na⁺ channel and (b) for the K⁺ channel. Channel conductance was measured for different depolarizing voltage steps away from the resting potential.

continuous-time membrane dynamics and channel kinetics in a fully digitally programmable and reconfigurable interface. Each neuron and synapse in the network offer individually programmable parameters setting reversal potentials, conductances, and voltage-dependent channel opening and closing rates. Least squares parameter fitting was shown to accurately reproduce biophysical neural data of channel opening and closing rates, gating variable dynamics, and action potentials. We further observed coupled neural spiking dynamics in a network with inhibitory synapses.

The implemented neural model extends on the HH formulation by allowing for arbitrary voltage profiles for channel

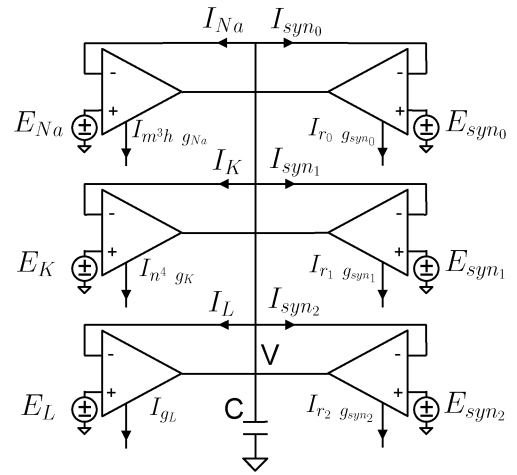


Fig. 11. Transconductance-C circuit implementing membrane dynamics for one neuron with synaptic input from the other three neurons.

opening and closing rates. The approach can be further extended by using similar principles to include adaptation mechanisms using calcium dynamics, and to implement resistively coupled multicompartment neurons. The work shown here represents a first step toward detailed silicon modeling of general neural and synaptic dynamics, combining digital and analog VLSI for maximum configurability and functionality.

APPENDIX A

DERIVATION OF THE CIRCUIT IMPLEMENTING KINETICS OF CHANNEL GATING VARIABLES

Here, we derive the dynamics of the circuit in Fig. 6 by implementing the kinetics in the channel gating variables by combining the α and β rate currents. The log-domain circuit [59] uses the dynamic translinear principle, exploiting the exponential current-voltage dependence of MOS transistors operating in the subthreshold region [56]. Drain currents are modeled as $I_d = I_0 W/L \exp((\kappa V_g - V_s)/V_T)$ in gate voltage V_g and source voltage V_s relative to the bulk, where V_T is the thermal voltage, kT/q and κ is the bulk back-gate effect factor [57]. The resulting translinear loop relation $I_{M1} I_{M3} = I_{M2} I_{M4}$ combined with Kirchhoff's current law leads to

$$I_\alpha I_{ref} = \left(I_\alpha + I_\beta + C \frac{d}{dt} (V_3 - V_1) \right) I_{out}. \quad (14)$$

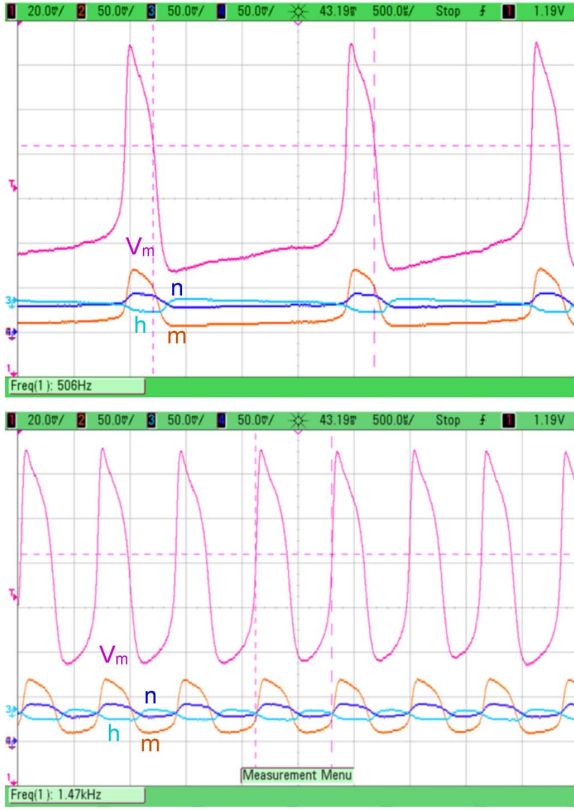


Fig. 12. Measured dynamics of membrane voltage V_m and gating variables n , m , and h for a single HH neuron. (a) and (b) show the effect of setting the global temporal scale parameter I_τ , uniformly speeding or slowing the dynamics across all variables.

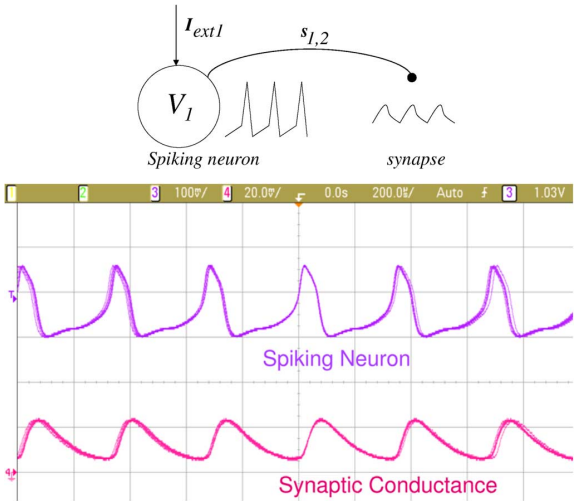


Fig. 13. (a) Synapse with presynaptic spiking neuron diagram (above). (b) Oscilloscope trace of the conductance curve of a synapse with a spiking presynaptic neuron input. Notice that the spiking neuron waveform (purple) and conductance curves for the synapse (pink) are in phase (below).

Since $I_{out}/I_{ref} = I_{M4}/I_{M3} = \exp(\kappa(V_3 - V_1)/V_T)$, the voltage dynamics of $V_3 - V_1$ in (14) are expressed in the current log domain as

$$\frac{d}{dt} \frac{I_{out}}{I_{ref}} = \frac{\kappa}{V_T} \frac{d}{dt} (V_3 - V_1) \frac{I_{out}}{I_{ref}} \quad (15)$$

leading to (11).

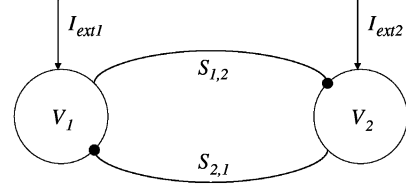


Fig. 14. Coupled neurons diagram. Two spiking neurons are connected with inhibitory synapses.

APPENDIX B

CALIBRATION PROCEDURE FOR α AND β PARAMETER FITTING

A. Rectified Linear Regression

Let $I_{meas}(V, I_{b1}, \dots, I_{b7})$ be the measured α or β function of V obtained with current bias parameter settings I_{b1}, \dots, I_{b7} . Then, for calibration, we measure the individual sigmoid contributions

$$I_{\sigma,k}(V) = I_{meas}(V, \delta_{k1}, \dots, \delta_{k7}) \quad (16)$$

where $\delta_{kj} = 1$ for $k = j$, and 0 otherwise. Hence, because of linearity in current summation, we may assume

$$I_{meas}(V, I_{b1}, \dots, I_{b7}) \approx \sum_{k=1}^7 I_{bk} I_{\sigma,k}(V). \quad (17)$$

To proceed, we perform a first linear fit of $I_{meas}(V, I_{b1}, \dots, I_{b7})$ to the target function $I_{target}(V)$ by using rectified linear least-squares regression in the coefficients I_{bk}

$$\min_{I_{b1}, \dots, I_{b7} \geq 0} : \sum_V \left(\sum_{k=1}^7 I_{bk} I_{\sigma,k}(V) - I_{target}(V) \right)^2. \quad (18)$$

The rectification is necessary because of the positivity constraints on the bias current parameters.

B. Iterative Linear Least-Squares Residue Correction

Next, we correct for residual errors due to nonlinearities in the current multiplying DACs by implementing the sigmoid weighting (17). To do so, we linearize the system around the current operating point, by regressing the residue to locally differential sigmoid contributions

$$\Delta I_{\sigma,k}(V) = I_{meas}(V, I_{b1} + \epsilon \delta_{k1}, \dots, I_{b7} + \epsilon \delta_{k7}) - I_{meas}(V, I_{b1}, \dots, I_{b7})$$

where ϵ is chosen sufficiently small for the linear analysis to be valid, but sufficiently large for reliable measurement. We proceed with another round of rectified linear least-squares regression in the parameters $I_{bk} + \Delta I_{bk}$ subject to the same positivity constraints, and iterate until the changes in parameter values ΔI_{bk} are small compared to the DAC precision.

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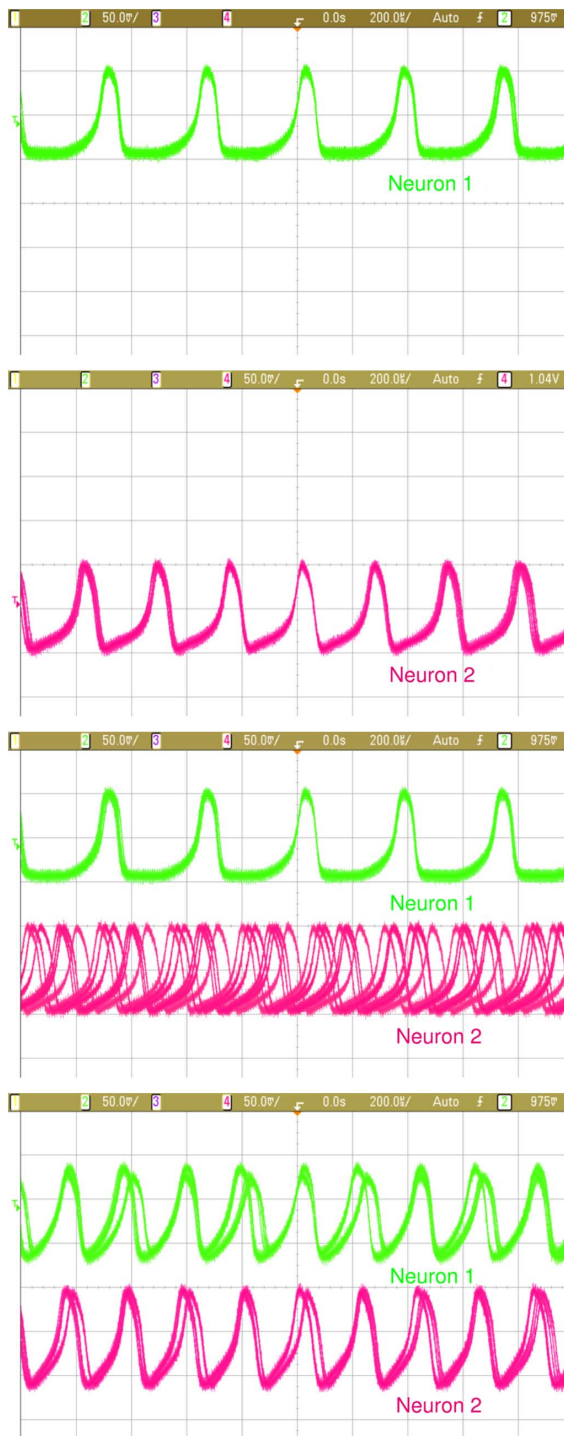


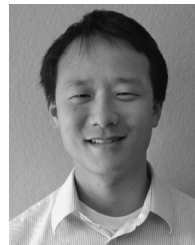
Fig. 15. Oscilloscope traces showing synaptic coupling in neural dynamics. (a) Through (c) individual uncoupled spiking neurons and (d) neurons coupled with inhibitory synapses spiking in synchrony.

from interactions with participants at the 2008 National Science Foundation Workshop on Neuromorphic Cognition Engineering in Telluride, CO.

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Theodore Yu (S'04) received the B.S. and M.S. degrees in electrical engineering from the California Institute of Technology, Pasadena, in 2004 and 2005, respectively, and is currently pursuing the Ph.D. degree in electrical and computer engineering at the University of California, San Diego.

His research interests include neuromorphic analog very-large scale integrated models of neural and synaptic circuits and circuit implementations of learning algorithms.



Gert Cauwenberghs (SM'89–M'94–SM'04) received the Ph.D. degree in electrical engineering from the California Institute of Technology, Pasadena.

Currently, he is Professor of Bioengineering at University of California, San Diego, where he co-directs the Institute for Neural Computation. Previously, he was Professor of Electrical and Computer Engineering at Johns Hopkins University, Baltimore, MD, and Visiting Professor of Brain and Cognitive Science at the Massachusetts Institute of Technology, Cambridge. His research interests cover neuromorphic engineering, computational and systems neuroscience, neuron-silicon and brain-machine interfaces, as well as learning and intelligent systems. He is Associate Editor for IEEE TRANSACTIONS ON BIOMEDICAL CIRCUITS AND SYSTEMS, and IEEE TRANSACTIONS ON NEURAL SYSTEMS AND REHABILITATION ENGINEERING. He is a Senior Editor for the IEEE SENSORS JOURNAL.

Dr. Cauwenberghs received the National Science Foundation Career Award in 1997, the ONR Young Investigator Award in 1999, and Presidential Early Career Award for Scientists and Engineers in 2000.